

A Unified Representation of Multi-Protein Complex Data for Modeling Interaction Networks

Chris Ding^{1*}, Xiaofeng He¹, Richard F. Meraz², Stephen R. Holbrook²
Computing Research Division¹ and Physical Biosciences Division²
Lawrence Berkeley National Laboratory, Berkeley, CA 94720
{chqding,xhe,rferaz,srholbrook}@lbl.gov

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Abstract

The protein interaction network presents one perspective for understanding cellular processes. Recent experiments employing high-throughput mass spectrometric characterizations have resulted in large datasets of physiologically relevant multi-protein complexes. We present a unified representation of such datasets based on an underlying bipartite graph model that is an advance on existing models of the network. Our unified representation allows for weighting of connections between proteins shared in more than one complex as well as addressing the higher level of organization that occurs when the network is viewed as consisting of protein complexes that share components. This representation also allows for the application of the rigorous MinMaxCut graph clustering algorithm for the determination of relevant protein modules in the networks. Statistically significant annotations of clusters in the protein-protein and complex-complex network using terms from the Gene Ontology suggest that this method will be useful for posing hypothesis about uncharacterized components of protein complexes or uncharacterized relationships between protein complexes.

Introduction

Proteins carry out most essential cellular processes in complex multi-protein assemblies. These protein complexes perform activities needed for metabolism, communication, growth and structure. A systematic identification, characterization and understanding of these molecular machines of life will provide an essential knowledge base and link proteome dynamics and architecture to cellular function and phenotype. A variety of experimental and computational approaches have been employed to deduce the constituents of protein macromolecular complexes. Experimental approaches such as the yeast two-hybrid genetic screen yield binary interaction data, while more recent high-throughput methods combine tagged “bait” proteins and protein complex purification schemes with mass spectrometric measurements to yield physiologically relevant data on intact multi-protein complexes [1, 2, 3, 4]. Taken together, data from these experiments approximate the network of interactions between proteins and protein complexes that govern most cellular processes.

An important issue is the effective representation of the functional relationships between various parts of the interaction network [5]. So far most studies have represented protein interaction data as a map of binary interactions with uniformly weighted connections between interacting proteins [6, 7]. For multi-protein complex data, this binary model assumes a pairwise interaction between all constituents in a complex. This

*Corresponding author.

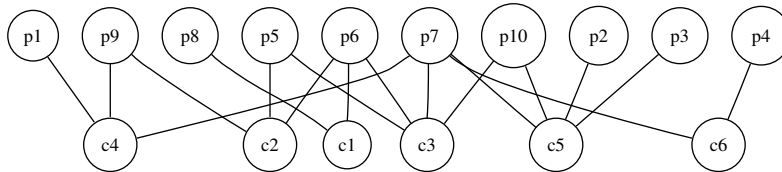


Figure 1: A bipartite graph representation of a hypothetical protein complex dataset. The p-nodes represent proteins and c-nodes represent experimentally-determined protein complexes. An edge between a p-node and a c-node indicates that the protein is contained in the protein complex.

equal weighting, however, is an oversimplification since physical interactions between constituents cannot be unambiguously described for all complexes without rigorous structural analysis. Some efforts have been made to improve upon the binary interaction model. The “spoke” model [7] assumes pairwise interactions only between the purification “bait” and proteins that co-purify in the complex. A hypergraph model extends the network structure to allow hyperedges corresponding to protein complexes to connect arbitrarily many proteins in the network [8].

The most important limitation of existing models of the protein interaction network is their inability to represent a higher order organization of the proteome that results from the consideration of network relationships between protein complexes. A recent review by Gavin and Superti-Furga discusses the major issues concerning protein complexes and proteome organization and gives several examples of the modularity of protein complexes and their ability to share components and interact in complex cellular processes [9]. A model of the protein interaction network that adequately deals with relationships between protein complexes would be an important step toward a framework for a systems-level understanding of cellular processes.

A Bipartite Graph Model of Protein Complex Data

We propose a novel representation of multi-protein complex data that treats proteins and protein complexes in a unified manner. This representation emphasizes the “duality” of the relationship: a protein complex is characterized by its constituent proteins, while the interaction between two proteins can be gauged by the number of protein complexes that contain these proteins. This duality is best captured by a bipartite graph (Figure 1) specified by an adjacency matrix B , in which a protein complex is represented by a column and a protein is represented by a row. This bipartite representation of a multi-protein complex dataset leads to a coherent framework for interaction networks: (1) The protein-protein (p-p) interaction network arises naturally. If we define the interaction strength between two proteins as the number of complexes that contain the two proteins, this interaction strength is given precisely by the adjacency matrix BB^T . (2) Importantly, a protein complex - protein complex (c-c) interaction network also arises from this representation. If we define the interaction strength between two protein complexes as the number of common proteins shared between them, then this interaction strength is given by the adjacency matrix B^TB . These interaction networks form a unified framework which overcomes two shortcomings of previous work: (a) The c-c interaction network yields a higher level organization of cellular processes. (b) The interaction strength of connections in the networks is more realistic than simple uniform weighting. See the *Methods* Section for more details.

The more quantitative interaction strength of network connections in our dual representation allows for the application of a rigorous graph clustering algorithm [10]. The goal of clustering the protein interaction network is to determine its component modules, their functional annotations and the relationships between them. A

module in a biological network is loosely defined as a functional unit separable from the rest of the network. In this context the terms “modules” and computationally discovered “clusters” are interchangeable. Our hypothesis is that such computationally discovered clusters would encompass proteins related through physical and possibly temporal associations in functionally coincident macromolecular complexes (p-p network), or reveal diverse relationships among cellular process composed of functionally related protein complexes (c-c network).

Methods

Protein Complex Data Can Be Modeled as a Bipartite Graph

The representation of a multi-protein complex dataset as a bipartite graph allows us to immediately infer a number of important quantities and to apply a large body of existing graph techniques.

A bipartite graph has two type of nodes: p-type nodes that denote proteins (or p-nodes) and c-type nodes that denote protein complexes (c-nodes). This graph structure only allows connections between p-nodes and c-nodes. Thus a protein complex (c-node) has edges connecting to each of its constituent proteins (p-nodes) (Figure 1). A bipartite graph is uniquely determined by its adjacency matrix $B = (b_{ij})$. Let c_1, c_2, \dots, c_n denote protein complexes and p_1, p_2, \dots, p_m denote constituent proteins. Define

$$b_{ij} = \begin{cases} 1 & \text{if protein } p_i \text{ is in protein complex } c_j \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

i.e., a protein complex is represented by a column in B where each entry is either 1 or 0 with a 1 indicating that the complex contains the protein of the corresponding row. Similarly, a protein is represented by a row in B . For consistency, we refer to the relationship between proteins and complexes represented by the bipartite graph as the p-c network. Starting from the p-c network, we can naturally obtain the following two networks.

Protein-Protein Interactions (p-p Network)

The interaction strength between two proteins p_i, p_j is

$$(BB^T)_{ij} = \left(\begin{array}{c} \# \text{ of protein complexes} \\ \text{containing both proteins } p_i, p_j \end{array} \right) \quad (2)$$

Note $(BB^T)_{ii} = \sum_j b_{ij} =$ the number of protein complexes that protein p_i is involved. We call this the weight of protein p_i .

Complex - Complex Associations (c-c network)

The interaction strength between two protein complexes c_i, c_j is

$$(B^TB)_{ij} = \left(\begin{array}{c} \# \text{ of proteins shared by} \\ \text{protein complexes } c_i, c_j \end{array} \right) \quad (3)$$

Note that $(B^TB)_{jj} = \sum_i b_{ij} =$ the number of proteins contained in the protein complex c_j . We call this the weight of protein complex c_j .

MinMaxCut Clustering

The MinMaxCut graph clustering algorithm [11] can be applied equally well to the p-p or c-c networks. Let the weight matrix $W = (w_{ij})$ denote the pairwise connection strength between proteins, or between protein complexes. We wish to partition the connection network G into two subnetworks G_1, G_2 , based on a min-max clustering principle. The total connection strength between G_1, G_2 is

$$s(G_p, G_q) = \sum_{i \in G_p} \sum_{j \in G_q} w_{ij}, \quad (4)$$

The total connection strength within a cluster G_1 or G_2 is similarly defined. The clustering principle requires minimizing $s(G_1, G_2)$ (weak connections between different clusters) while simultaneously maximizing $s(G_1, G_1)$ and $s(G_2, G_2)$ (strong connections within each cluster). These requirements are satisfied by the objective function,

$$J(G_1, G_2) = \frac{s(G_1, G_2)}{s(G_1, G_1)} + \frac{s(G_1, G_2)}{s(G_2, G_2)}. \quad (5)$$

The solution of the clustering problem is represented by an indicator vector \mathbf{q} , where the i^{th} entry of \mathbf{q} is

$$q(i) = \begin{cases} a & \text{if } i \in G_1 \\ -b & \text{if } i \in G_2 \end{cases} \quad (6)$$

where a and b ($0 < a, b < 1$) are constants. One can prove that

$$\min_{\mathbf{q}} J(G_1, G_2) \Rightarrow \min_{\mathbf{q}} \frac{\mathbf{q}^T (D - W) \mathbf{q}}{\mathbf{q}^T D \mathbf{q}}, \quad (7)$$

where $D = (d_i)$ is a diagonal matrix, $d_i = \sum_j w_{ij}$. Now, relaxing $q(i)$ from discrete indicator in Eq.6 to a continuous values in $[-1, 1]$, the solution \mathbf{q} of the minimization problem satisfies

$$(D - W)\mathbf{q} = \lambda D\mathbf{q}. \quad (8)$$

The desired solution is the eigenvector \mathbf{q}_2 corresponding to the second smallest eigenvalue. From Eq.6, we can recover clusters by the sign of \mathbf{q}_2 , i.e., $G_1 = \{i \mid q_2(i) \leq 0\}$, $G_2 = \{i \mid q_2(i) > 0\}$. In general, the optimal dividing point could shift away from 0; we search the dividing point $q(i_{cut})$

$$G_1 = \{i \mid q(i) \leq q(i_{cut})\}, \quad G_2 = \{i \mid q(i) > q(i_{cut})\}.$$

($i_{cut} = 1, \dots, n-1$) such that $J(G_1, G_2)$ is minimized (the minimum value is J^{opt}). This gives the final clusters G_1 and G_2 .

Hierarchical Divisive Clustering

Divisive clustering starts from the top by treating the whole dataset as a single initial cluster. It recursively splits the current cluster (a leaf node in a binary clustering tree) into two sub-clusters. Two important issues are: (1) how to select the next candidate cluster to split and (2) when to terminate the recursive process.

Given a current cluster G_k , we wish to decide whether to further split it into two sub-clusters. We apply MinMaxCut to G_k . If J^{opt} is large then the overlap between two resulting sub-clusters is large in comparison to the within-sub-cluster similarity and hence cluster G_k should not be further split. Thus the optimal value J^{opt} is a measure of “cluster cohesion”.

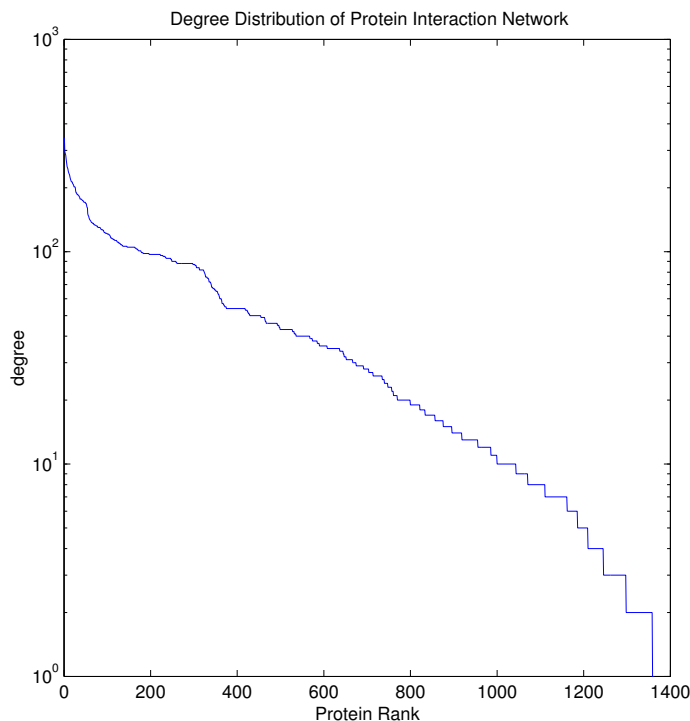


Figure 2: Distribution of the degree (number of proteins a given protein interacts with) in the protein-protein interaction network. This curve approximates a power-law distribution indicating that it is a scale-free network topology.

At every cluster splitting in the divisive process we compute the cluster cohesion for each of the sub-clusters. To select the next cluster to split, we select among all current clusters the one with the smallest cohesion. As the cluster splitting process continues, clusters with small cohesion are split and the cohesion of the resulting clusters increases. To terminate the divisive process, we set a threshold for cohesion $h = 0.6$, i.e., clusters with cohesion greater than h will not be split further. A greater cohesion threshold will lead to “tighter” clusters. h is the only parameter in the MinMaxCut algorithm.

Resources

(1) The February 2003 release of the Gene Ontology (GO) (<http://www.geneontology.org>) was used to obtain the annotated terms for yeast proteins from the TAP-MS dataset [4]. (2) A freely distributed perl library interface to the Gene Ontology database [12] was employed for all calculations relating to GO annotations and (3) a perl library interface to the GraphViz package [13] was used to create the graph representations. (4) The primary sequences for all proteins analyzed were obtained from the Saccharomyces Genome Database [14]. (5) The EMBOSS toolkit [15] was used for calculations of sequence properties and (6) the PsiPred program [16] was used for secondary structure determination. (7) A website with additional results related to this paper is located at <http://frna.lbl.gov/complex>.

Results and Discussion

Multi-Protein Complex Dataset

Two datasets summarizing high-throughput analysis of multi-protein complexes are available for the yeast *Saccharomyces cerevisiae*. Coupling different purification (immunoprecipitation and tandem affinity purification (TAP)) and labeling schemes with mass spectrometry (MS), both studies used bait proteins to identify physiologically intact protein complexes [3, 4]. A recent analysis used a maximum likelihood model and gene expression correlation coefficients to evaluate the reliability of various high-throughput protein-protein interaction datasets and concluded that the TAP-MS dataset had the highest accuracy for predicting protein function [17]. Another analysis compared the accuracy and coverage of protein interactions for several high-throughput datasets relative to trusted reference sets of manually annotated protein complexes from the Munich Information Center for Protein Sequences (MIPS) and the Yeast Proteome Database (YPD) [18]. This analysis also revealed a superior accuracy to coverage tradeoff for the TAP-MS data relative to other methods. Hence we have chosen this dataset to illustrate our model. More information about the TAP-MS dataset is available at <http://yeast.cellzome.com>.

We represent this dataset as a bipartite graph with adjacency matrix B . The symmetric matrix BB^T defines the interaction strength of the protein-protein interaction network from the underlying bipartite graph model. This p-p network shows a scale free topology indicating that proteins in the network have a wide range of connectivities (Figure 2). Previous work has speculated that connectivity in the network might correlate with observable biological properties such as the rate of protein evolution [19].

Clusters in the p-p Interaction Network Define Modules of Protein Complexes

Given a network of protein interactions, one can computationally predict modules and annotate these modules with a biological context. A computationally predicted protein module is defined as a highly connected region or structure in the network. Previous work has employed “ k -cores” and other density-based methods to partition the protein interaction network [7, 20]. In this paper we identify clusters in the protein interaction network using a graph clustering algorithm, MinMaxCut, which was shown to be effective for class discovery in gene expression microarray data for lymphoma [10] (see *Methods* section). We apply MinMaxCut to the protein interaction network specified by the adjacency matrix BB^T . The non-uniform interaction strength between proteins gives a more realistic characterization of the network. Following, we present an analysis of the p-p interaction network, highlighting only the main results. A comprehensive analysis of these results is deferred to a later paper.

Figure 3 shows the interaction strength (the adjacency matrix BB^T) of the p-p network sorted after clustering. Several clusters exhibit high overall interaction strength and most encompass biologically meaningful complexes. To support our supposition that clusters in the p-p network encompass physiologically relevant protein complexes we compared the discovered p-p clusters to the TAP-MS protein complexes that are the basis of the bipartite graph model. To quantify this correspondence we define the match coefficient

$$\rho = n(P_k, c_j) / \min(|P_k|, |c_j|)$$

where $|P_k|$ = number of proteins in p-p cluster P_k , $|c_j|$ = number of proteins in TAP-MS protein complex c_j , and $n(P_k, c_j)$ = number of shared proteins between P_k and c_j . The constituents of a protein cluster P_k may all be contained in an experimental protein complex c_i ; or conversely, the constituents of c_i may all be contained

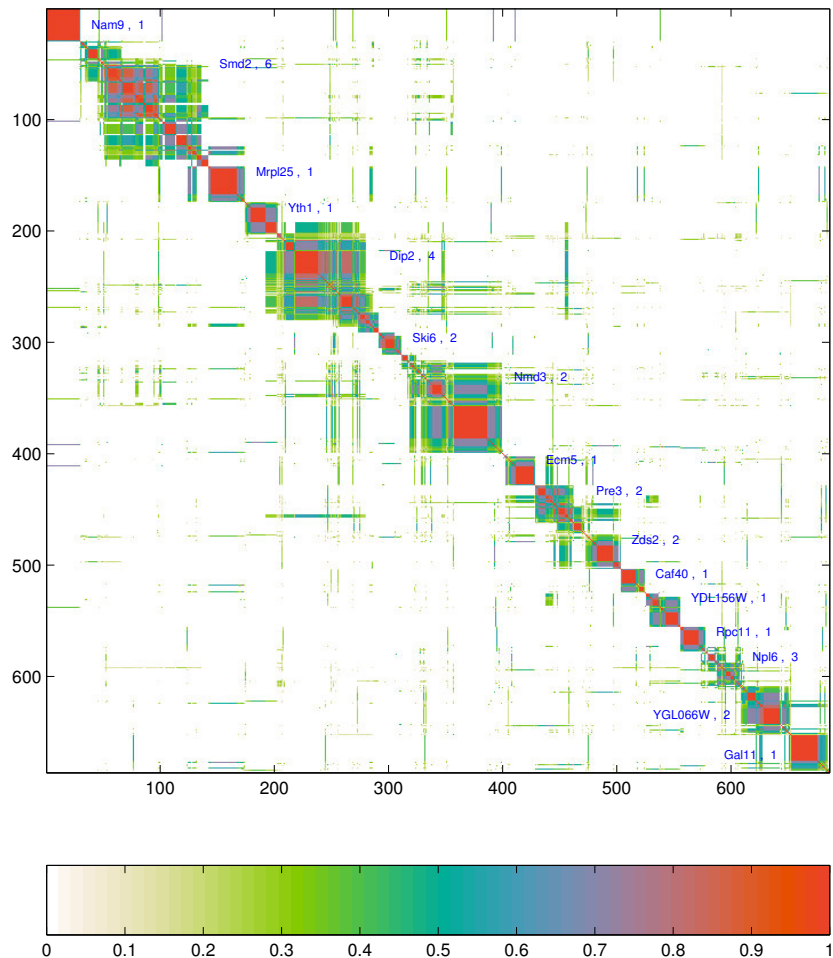


Figure 3: Predicted clusters of the p-p network. The color shows the normalized interaction strength of connections in the p-p network. Clusters with less than 20 proteins are not shown. The most highly connected protein in each cluster is shown by its protein name and the number of TAP-MS protein complexes this cluster matches (with $\rho > 0.7$) is shown after the protein name. Axes correspond to proteins. For example, cluster P_{28} with protein Smd2 has 112 proteins and overlaps 6 TAP-MS protein complexes. A larger figure showing all clusters is available, see *Methods* section, Resources (7).

in P_k ; both cases result in a perfect match with $\rho = 1$. Using this match coefficient and a threshold of 0.7 we found that 65 of 66 predicted p-p clusters match to at least one experimental protein complex (Figure 4). This is strong evidence that clusters in the p-p network define modules of physiologically intact protein complexes and furthermore that any clustered assemblies with uncharacterized constituents might correspond to novel interactions or functional relationships. Clearly those protein clusters which match two or more TAP-MS protein complexes are most interesting. For example, Figure 5 details how the largest cluster in the p-p network denoted P_{28} (labeled with Smd2 in Figure 3) matches six TAP-MS protein complexes. These matching complexes are also shown as six points in Figure 4 indicated by the arrow.

Modules in the p-p Network Have Characteristic Physical and Chemical Properties

The assembly, thermodynamic stability, and functionality of protein complexes are controlled by various environmental conditions in the cell. Surface accessible amino acid residues can be covalently modified to regulate the functional state of protein complexes. Non-covalent ligand binding can also modulate the functional state

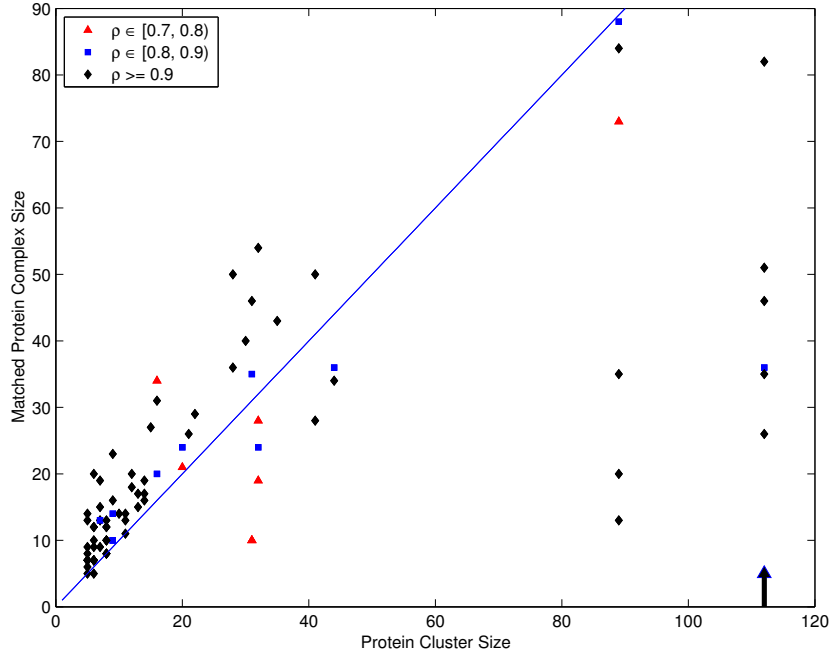


Figure 4: A summary of the overlap between the constituents of predicted p-p clusters and TAP-MS protein complexes. Match coefficients are indicated by the symbols. The solid line indicates where protein complexes and p-p clusters are of the same size. The arrow indicates the complexes that overlap a p-p cluster, designated P_{28} , which is discussed in the text.

Lys	100	Asn	56	Val	30	Ile	24
Asp	89	Gln	50	Tyr	29	Ser	23
Arg	73	Cys	39	Met	29	Leu	22
Pro	70	His	33	Trp	28	Gly	21
Glu	66	Ala	31	Thr	28	Phe	21
pI	169	Basic	149	Acidic	97	MW	60
Aromatic	30	Helix	37	Beta-Sheet	33	Coil	27

Table 1: F -statistics of amino acid composition (top) and physical properties (bottom) across all clusters in p-p interaction network.

of protein complexes. Hence we would expect that the proteins of discovered clusters in the p-p network would be distinguishable by intrinsic physical and chemical characteristics. We calculated an F -statistic for protein physical-chemical properties and amino acid composition to see if protein clusters exhibit any significant trends that might suggest distinguishing features of their interactions. Given a particular property f across n proteins and K clusters containing these proteins the F -statistic is defined as

$$F = \frac{1}{K-1} \sum_{k=1}^K n_k (\bar{f}_k - \bar{f})^2 / \frac{1}{n-K} \sum_{k=1}^K (n_k - 1) \sigma_k^2$$

where \bar{f} is the average across all proteins, \bar{f}_k and σ_k are the average and variance within p-p cluster P_k , and n_k is the size of cluster P_k . The magnitude of the F -statistic is a measure of how well the given property distinguishes between clusters. The various properties and their F -statistics are listed in Table 1. To assess the statistical significance, we compute the F -statistic for the same dataset when proteins are randomly assigned

P_28	C_128	C_129	C_155	C_158	C_160	C_161
YNL224C	YNL224C					
YML117W		YML117W				
YML025C						YML025C
YLR424W	YLR424W		YLR424W	YLR424W	YLR424W	YLR424W
YKL214C		YKL214C				
Yju2			Yju2			
YJR084W			YJR084W	YJR084W	YJR084W	YJR084W
YHR156C						YHR156C
Yhc1			Yhc1	Yhc1		Yhc1
YGR278W						YGR278W
YGL128C	YGL128C		YGR278W			YGL128C
YDL209C			YGL128C			YDL209C
YDL175C		YDL175C	YDL209C	YDL209C		YDL209C
YCR063W			YCR063W			YCR063W
Tos4						Tos4
Tif4632		Tif4632			Tif4632	
Tif4631		Tif4631			Tif4631	
Syl1			Syl1			Syl1
Sto1		Sto1	Sto1	Sto1		Sto1
Sro9	Sro9	Sro9				
Sro2				Srb2	Srb2	Srb2
Spp381						Spp381
Shu71		Shu71		Shu71	Shu71	Shu71
Snu66	Snu66	Snu56		Snu66	Snu66	Snu66
Snu56				Snu56	Snu56	Snu56
Snu23	Snu23			Snu56	Snu56	Snu23
Snu114	Snu114		Snu114	Snu114	Snu114	Snu114
Snt309			Snt309	Snt309	Snt309	Snt309
Snp1		Snp1	Snp1	Snp1	Snp1	Snp1
Smx3			Smx3	Smx3	Smx3	Smx3
Smx2			Smx2	Smx2	Smx2	Smx2
Sme1			Sme1	Sme1	Sme1	Sme1
Smd3		Smd3	Smd3	Smd3	Smd3	Smd3
Smd2	Smd2	Smd2	Smd2	Smd2	Smd2	Smd2
Smd1		Smd1		Smd1	Smd1	Smd1
Smb1	Smb1		Smb1	Smb1	Smb1	Smb1
Slu7						Slu7
Sgv1		Sgv1				
Sen1		Sen1				
Scp160		Scp160				
Rse1		Rse1	Rse1	Rse1	Rse1	Rse1
Rlr1		Rlr1				
Prp9			Prp9	Prp9	Prp9	Prp9
Prp8						Prp8
Prp6	Prp6		Prp6	Prp6	Prp6	Prp6
Prp46	Prp46		Prp46	Prp46	Prp46	Prp46
Prp45						
Prp43	Prp43		Prp43	Prp43	Prp43	Prp43
Prp42		Prp42	Prp42	Prp42	Prp42	Prp42
Prp40		Prp40	Prp40	Prp40	Prp40	Prp40
Prp4	Prp4		Prp4	Prp4	Prp4	Prp4
Prp39	Prp39	Prp39	Prp39	Prp39	Prp39	Prp39
Prp38	Prp38					Prp38
Prp31	Prp31		Prp31	Prp31	Prp31	Prp31
Prp3			Prp3	Prp3	Prp3	Prp3
Prp28						Prp28
Prp24	Prp24					Prp24
Prp22			Prp22			
Prp21			Prp21	Prp21	Prp21	Prp21
Prp2			Prp2			
Prp19			Prp19	Prp19	Prp19	Prp19
Prp18						Prp18
Prp11			Prp11	Prp11	Prp11	Prp11
Pat1	Pat1					Pat1
Nup60		Nup60				
Npl3		Npl3			Npl3	
Nam8		Nam8			Nam8	
Nam7	Nam7					
Nab3		Nab3				
Mud1		Mud1	Mud1	Mud1	Mud1	Mud1
Msl1			Msl1	Msl1	Msl1	Msl1
Msh4		Msh4				
Mrp5						Mrp5
Mrp18						Mrp18
Mrp14						Mrp14
Mrp138						Mrp138
Mrp135						Mrp135
Mrp13						Mrp13
Mrp128						Mrp128
Mrp7						Mrp7
Luc7		Luc7	Luc7	Luc7	Luc7	Luc7
Lsm7	Lsm7					Lsm7
Lsm6	Lsm6					Lsm6
Lsm5	Lsm5		Lsm4	Lsm4	Lsm4	Lsm4
Lsm4	Lsm4					
Lsm3	Lsm3					
Lsm2	Lsm2					Lsm2
Lsm1	Lsm1					Lsm1
Lea1			Lea1	Lea1	Lea1	Lea1
Krs1	Krs1		Lea1			
Isy1			Isy1			
Img1						Img1
Hta1		Hta1				Hta1
Hsh49			Hsh49	Hsh49	Hsh49	
Hsh155			Hsh155	Hsh155	Hsh155	Hsh155
Hrt2			Hrt2			
Gcn2						Gcn2
Ecm2			Ecm2	Ecm2	Ecm2	Ecm2
Dib1	Dib1		Dib1	Dib1	Dib1	Dib1
Dhh1	Dhh1					Dhh1
Cus1	Cif1		Cus1	Cus1	Cus1	Cus1
Cif1	Cif1		Cif1	Cif1	Cif1	Cif1
Cef1			Cef1	Cef1	Cef1	Cef1
Cdc40			Cdc40			
Cdc33	Cdc33			Cdc33	Cdc33	Cdc33
Cbc2		Cbc2		Cbc2	Cbc2	
Bur2		Bur2				
Brr1		Brr1		Brr1	Brr1	Brr1
Aar2						Aar2
Nrp1	Asc1	Kap95			Yef3	Rvb2
Pub1	Dcp2	Nrd1				YLR409C
Sgn1	Erb1	Srp1				
	Nop1					
	YER066W					
	YNR053C					

Figure 5: Protein cluster P_{28} matches six TAP-MS protein complexes (labeled as published [4]). All proteins in the cluster and matched protein complexes are listed. Proteins shared by the p-p cluster and at least one TAP-MS experimental protein complex are listed above the dividing line. Below the line are proteins not shared. The match coefficients are $\rho(P_{28}, c_{128}) = 0.83$, $\rho(P_{28}, c_{129}) = 0.91$, $\rho(P_{28}, c_{155}) = 1$, $\rho(P_{28}, c_{158}) = 1$, $\rho(P_{28}, c_{160}) = 0.98$, $\rho(P_{28}, c_{161}) = 0.98$.

to clusters. The F -statistic for randomly shuffled data are approximately 16 ± 8 across these quantities. Thus an F -statistic above 30 is significant.

Protein complexes can be characterized as non-obligate (temporary) or permanent where the native state is oligomeric. The surfaces that mediate the interactions in these two types of complexes necessarily differ in structural and physical properties [21]. Since using different values for the cluster cohesion parameter (See *Methods* section) of the MinMaxCut clustering algorithm is likely to result in discovered protein clusters that encompass differing ratios of these two types of complexes we would expect that the calculated physical properties would be somewhere intermediate between those expected for the two types of complexes. Indeed, this seems to be the case if we consider the F -statistics for amino acid composition. Interactions in temporary protein complexes which function dynamically in cellular processes are often tuned by the effects of polar groups (Lys, Arg, Gln, Asn, Asp) which define a complementary electrostatic surface, hydrogen bonding (Arg) and stabilizing hydrophobic interactions (proline). Methylation of Arg and Lys, and acetylation of Lys are well known covalent modifications of surface amino acids that could influence complex formation. Cys participates in the formation of disulfide bridges that can stabilize more permanent complexes as well as more dynamic interactions [22, 23]. Finally studies have shown that secondary structural features are often uniformly distributed at protein interaction interfaces which is consistent with their relative unimportance in the above calculations [21].

Supercomplexes Encompass Modules from the p-p Network

In previous analyses of protein complex data only the resulting pairwise interaction network has been examined [18, 7, 6]. The pairwise interaction network, however, yields an incomplete and noisy version of proteomic organization. As evidenced by recent high-throughput experiments for determining protein complexes: protein complexes are apt to share components and hence define a network of interconnected cellular processes [9]. No study to date has adequately represented the higher order organization of this network. In our dual representation of the data, the adjacency matrix $B^T B$ defines the connectivity between protein complexes where the connection is weighted by the number of shared proteins. Figure 6 shows the result of a MinMaxCut clustering of this network. Clusters are labeled with the most frequently occurring proteins as well as the number of TAP-MS protein complexes corresponding to a particular biological process [4]. We introduce the terminology “supercomplex” to denote a cluster in the complex-complex association network.

Since we expect supercomplexes to represent the diversity of interconnected cellular processes it would be consistent if each supercomplex showed high match coefficients with various modules from the p-p interaction network. Figure 7 summarizes the overlap between predicted supercomplexes and predicted clusters in the p-p interaction network. Most supercomplexes show overlap with several predicted p-p clusters and, in some instances, the same predicted p-p cluster occurs in multiple supercomplexes. In one instance the TAP-MS complexes overlapping a cluster in the p-p network and the TAP-MS complexes contained in a supercomplex are in one to one correspondence (P_{28} listed in Figure 5).

Computationally Discovered Modules are Biologically Consistent

We provide here preliminary evidence that computationally discovered modules in the dual representation are biologically consistent. To determine a biological context we used a set of controlled vocabularies defined by the Gene Ontology for which most of the proteins in our dataset have been annotated with at least one term [14]. The Gene Ontology consists of three orthogonal ontologies: biological process, molecular function and

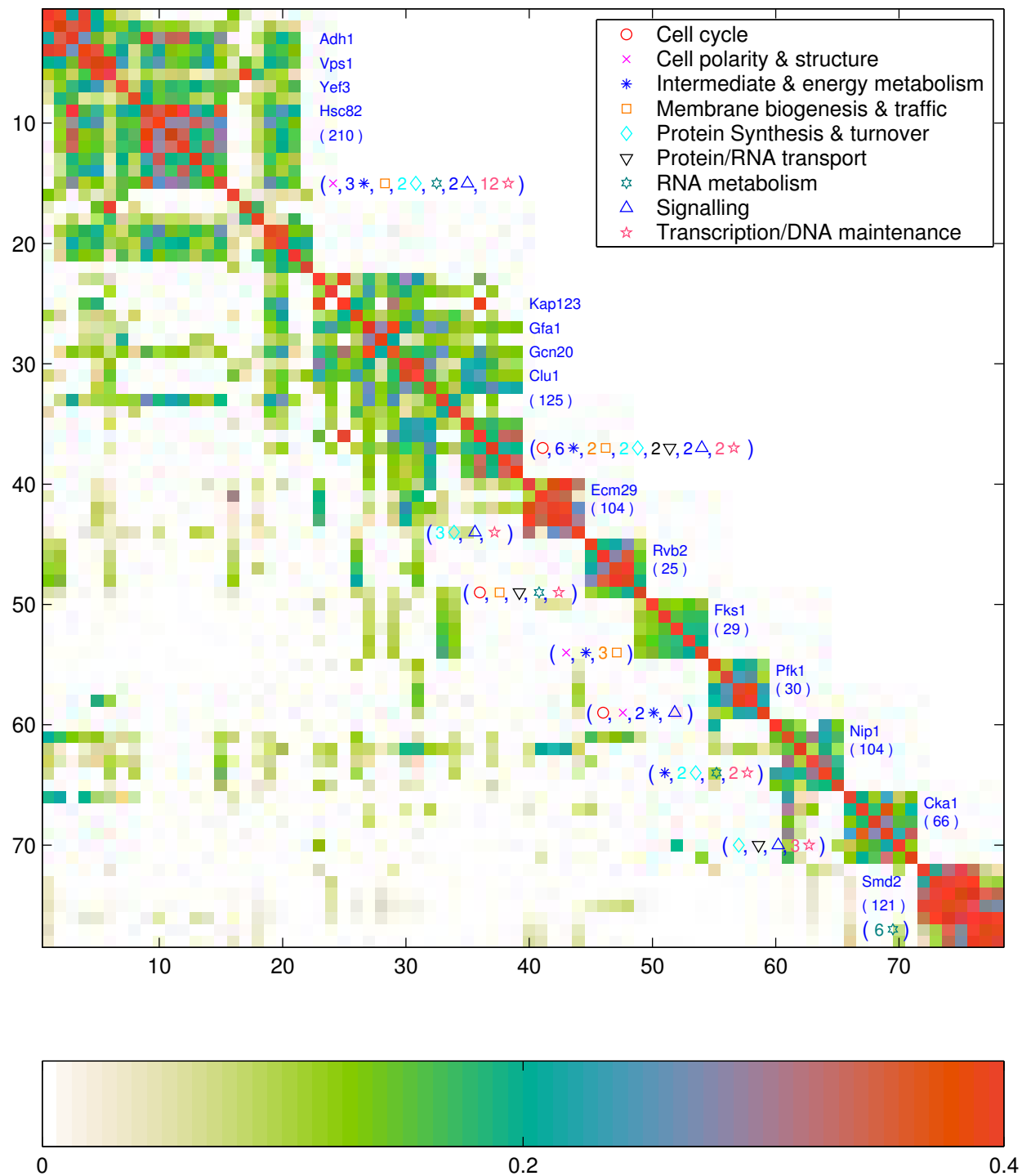


Figure 6: Predicted protein supercomplexes (clusters of the c-c network). Several large supercomplexes are shown. Each supercomplex is labeled with the most frequently occurring proteins, the number of non-redundant constituent proteins, and the relevant biological processes inferred from the participating TAP-MS experimental protein complexes. Axes correspond to TAP-MS complexes. Color represents normalized connection strength. A larger figure showing all clusters is available, see *Methods* section, Resources (7).

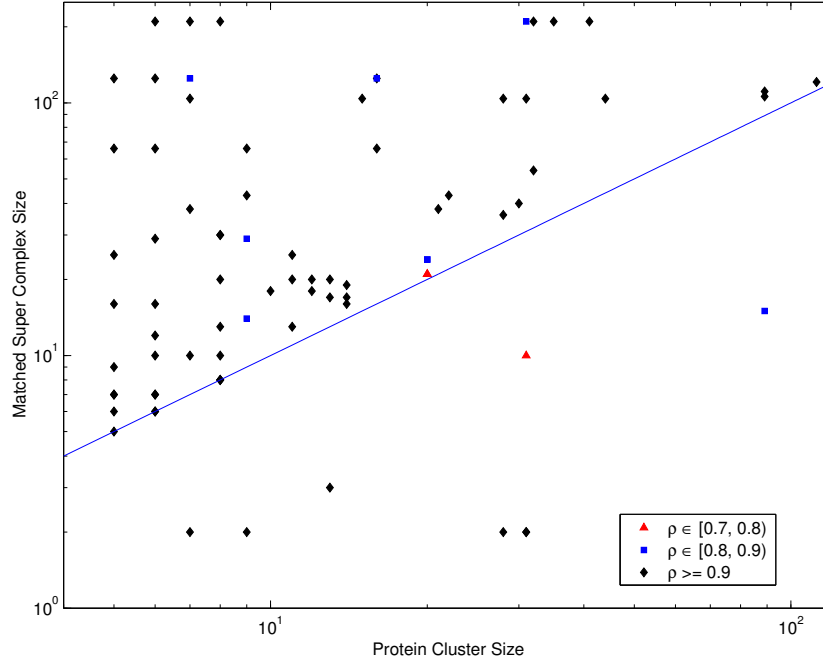


Figure 7: Overlap between computed supercomplexes (clusters of c-c network) and predicted clusters in the p-p network. The match coefficients defined by shared protein constituents are indicated.

cellular component [24]. Given that p-p clusters are defined by the proteins sharing maximal membership within the same experimentally determined protein complexes and c-c clusters capture relationships between protein complexes, we would expect the cellular component and biological process ontologies to give the most coherent annotations. We map each protein in a p-p cluster to the most specific ontological term assigned to it. For c-c clusters we determine a non-redundant union of all protein constituents and map these to their most specific annotated terms. The GO ontologies are organized as directed-acyclic graphs. This data structure allows us to ascend the graph from more specific terms to determine the set of common “parent” terms that describe a predicted cluster’s functional categories. We approximate the significance of that annotation by calculating the probability that n or more proteins would be assigned to that term if we assigned proteins randomly to the cluster. This probability is calculated as

$$P = \sum_{n \leq j \leq N} \binom{N}{j} p^j (1-p)^{N-j}$$

where p is ratio of proteins in the genome annotated to the given term, n is the number of proteins in the cluster annotated to the term, and N is the number of proteins in the cluster. This P-value allows us to rank annotations according to significance and to reason about the cellular roles for a given cluster. If a subgraph composed from the significant terms is biologically consistent, that infers the validity of the computationally determined module.

We briefly present two examples: the largest cluster in the p-p network denoted P_{28} and the largest cluster in the c-c network denoted C_{47} . Since these large clusters encompass proteins with a range of connection weights in the respective networks and hence probably encompass proteins and complexes of diverse function, we believe that they represent difficult examples to assign biological significance, and therefore adequately demonstrate the robustness of our method. P_{28} contains 112 proteins as depicted in Figure 5. Figure 8 shows the most significant ontological terms from the cellular component ontology corresponding to the proteins in

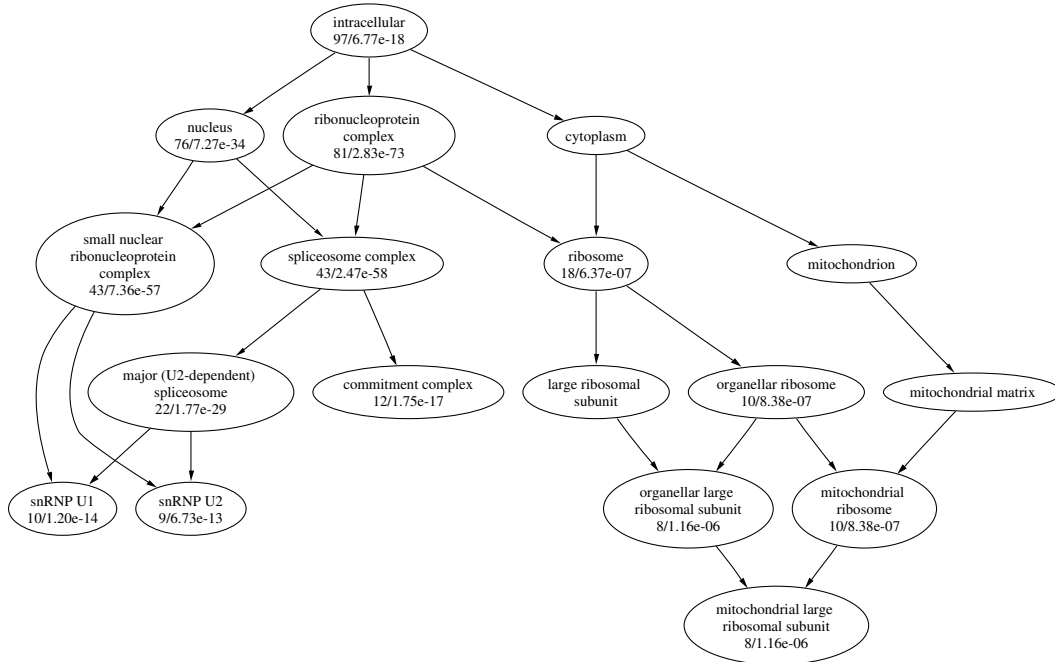


Figure 8: Subgraph of the gene ontology (Component) corresponding to a subset of the most prevalent annotations of proteins in p-p cluster P_{28} . Significant nodes are labeled with the number of proteins annotated directly or indirectly to that term and the P-value for the term.

this cluster. Annotations to the general terms nucleus (76 proteins) and ribonucleoprotein (RNP) complex (81 proteins) as well as more specific terms such as spliceosome complex (48 proteins), major (U2 dependent) spliceosome (22 proteins) and commitment complex (12 proteins) clearly indicate that these proteins are components of the pre-mRNA splicing machinery. It is known that the transcriptional machinery consists of several coupled multi-protein machines that carry out separate steps in gene expression coordinated via interactions with the carboxy terminal domain of the RNA polymerase II large subunit [25].

The predicted protein cluster P_{28} is also the only p-p cluster that corresponds exactly with a supercomplex. While most of the proteins in the cluster have been accounted for in stable complexes, there are also some more hypothetical relationships suggested by the GO annotations. For example, ten proteins are annotated to be associated with the mitochondrial ribosome. Constituents of the mitochondrial ribosome are encoded in both the nuclear and mitochondrial genomes. A mechanism that coordinates the expression of these constituents has been hypothesized, given that the stoichiometric synthesis of all mitochondrial ribosomal components is likely to be regulated to avoid wasting metabolic energy [26]. Hence the clustering of these proteins suggests a possible coupling between gene expression in the nucleus and mitochondria. Additionally, there is evidence that splicing can enhance export of mRNA from the nucleus [27] and that combinatorial binding of heterogeneous ribonucleoproteins to mRNA may regulate post-transcriptional events such as nuclear export, mRNA stability, and nonsense mediated decay [28]. That many of our proteins are annotated to these terms (commitment complex, mRNA-nucleus export, translation initiation, polysome, cytoplasmic transport, mRNA splicing) at least suggests these relationships and their interdependence. See the *Methods* section, Resources (7) for a complete list of annotations.

The largest supercomplex C_{47} illustrates how diverse cellular process can be coupled via a nexus of interconnected protein complexes. Figure 9 shows the most significant GO-process annotations for this supercomplex

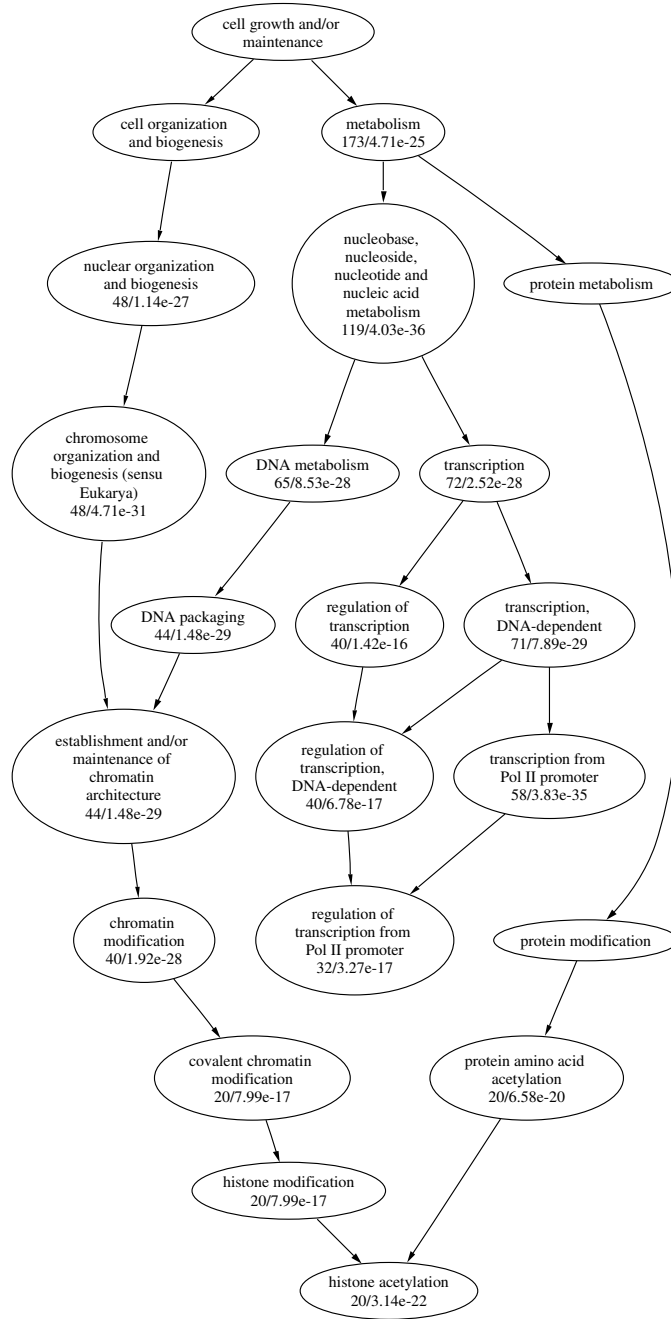


Figure 9: Subgraphs of the gene ontology (Process) corresponding to a subset of the most prevalent annotations of proteins in supercomplex C_{47} . Significant nodes are labeled with the number of proteins annotated directly or indirectly to that term and the P-value for the term.

(210 proteins). The GO-process annotations suggest that this supercomplex encompasses complexes involved in chromatin dynamics and transcriptional regulation and initiation as well as cell cycle control, DNA replication and repair, and signal transduction (for clarity only a subset of the significant annotations are shown in Figure 9). See the *Methods* section, Resources (7) for a complete annotation. We determined a list of curated protein complexes from the MIPS Catalog (<http://mips.gsf.de>) that are highly represented in the supercomplex. A subset of this list is shown in Table 2. Several of these complexes are known chromatin regulators in yeast (see highlighted complexes in Table 2) and are necessary for such processes as transcriptional initiation,

MIPS Listing	# ORFs	# ORFs in C_{47}
RNA Pol II holoenzyme	35	23
Kornberg’s mediator	21	21
Other transcription	73	17
HAT A	15	14
TFIID	13	13
SAGA	14	13
Ada-Spt	14	13
TAFIIIs	12	12
DNA repair	33	9
RSC	10	6
ADA	6	6
Replication fork	30	6
DNA mismatch repair	5	5
Cytoplasmic translation initiation	27	4
SAGA-like	5	4
Nucleotide excision repairosome	16	3
RNA Polymerase III	13	3
Replication factor A	3	3
Actin-associated motorproteins	7	3
MSH2/MSH3	3	3
Srb10p	4	3
NEF4	2	2
eIF4A	2	2
NuA4	2	2
Nuclear pore	24	2
Sir	2	2

Table 2: A sample of known protein complexes from the curated MIPS catalog which have many constituents in supercomplex C_{47} . Listed are the name of the complex, the number of known ORFs in the complex, and the number of ORFs from the complex present in C_{47} . Rows containing complexes implicated in chromatin dynamics are shaded [29].

certain types of DNA repair and silencing mechanisms, and cell cycle progression [30, 31, 32].

Conclusion

In this paper we propose a dual representation that unifies three interaction networks, the protein - protein complex (p-c) network, the protein - protein interaction (p-p) network and the protein complex - protein complex (c-c) network under a single framework. The resulting protein - protein and complex - complex interaction networks have more realistic interaction strengths compared to the conventional binary interaction networks with equal weighting. This results in a coherent framework for computational detection of modules which occur as clusters or densely connected regions in the dual representations. We apply a rigorous graph clustering algorithm to find these modules. Basic statistical analysis revealed that differences between modules in the protein interaction network are reflected by characteristic physical and chemical properties of the protein interactions. We emphasize the protein complex - protein complex ($B^T B$) network as reflecting a higher-order organization of the proteome. The largest supercomplex has 210 non-redundant constituent

proteins and is involved in a number of cellular processes. Use of the Gene Ontology revealed that the biological annotations of computationally discovered modules are statistically significant and that this method can facilitate the functional annotation of uncharacterized constituents in future multi-protein complex datasets as well as the discernment of novel functional relationships between protein complexes. As more and higher quality protein complex data becomes available, we expect this unified representation of interaction networks and associated clustering methodology to evolve into a useful framework for studying this aspect of systems biology.

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References

1. Uetz, P., Giot, L., Cagney, G., Mansfield, T. A., Judson, R. S., Knight, J. R., Lockshon, D., Narayan, V., Srinivasan, M., Pochart, P., et al. A comprehensive analysis of protein-protein interactions in *Saccharomyces cerevisiae*. *Nature* 403:623–627, February, 2000.
2. Ito, T., Chiba, T., Ozawa, R., Yoshida, M., Hattori, M., and Sakaki, Y. A comprehensive two hybrid analysis to explore the yeast protein interactome. *Proceedings of the National Academy of Sciences* 98(8):4569–4574, April, 2001.
3. Ho, Y., Gruhler, A., Heilbut, A., Bader, G., Moore, L., Adams, S.-L., Millar, A., Taylor, P., Bennett, K., Boutillier, K., et al. Systematic identification of protein complexes in *Saccharomyces cerevisiae* by mass spectrometry. *Nature* 415:180–193, October, 2002.
4. Gavin, A.-C., Bosche, M., Krause, R., Grandi, P., Marzioch, M., Bauer, A., Schultz, J., Rick, J. M., Michon, A.-M., Curciat, C.-M., et al. Functional organization of the yeast proteome by systematic analysis of protein complexes. *Nature* 415:141–147, 2002.
5. Alm, E. and Arkin, A. P. Biological networks. *Current Opinion in Structural Biology* 13:193–202, 2003.
6. Schwikowski, B., Uetz, P., and Fields, S. A network of protein-protein interactions in yeast. *Nature Biotechnology* 18:1257–1261, December, 2000.
7. Bader, G. D. and Hogue, C. W. V. Analyzing yeast protein-protein interaction data obtained from different sources. *Nature Biotechnology* 20:991–997, October, 2002.
8. Pothén, A. Graph and hypergraph models of protein interaction networks, , 2003.
9. Gavin, A.-C. and Superti-Furga, G. Protein complexes and proteome organization from yeast to man. *Current Opinion in Chemical Biology* 7:21–27, 2003.
10. Ding, C. Analysis of gene expression profiles: class discovery and leaf node ordering. In *Proc. 6th Int’l Conf. Comp. Mol. Bio. (RECOMB)*, 127–136, , 2002.
11. Ding, C., He, X., Zha, H., Gu, M., and Simon, H. A min-max cut algorithm for graph partitioning and data clustering. In *Proc. IEEE Int’l Conf. Data Mining (ICDM)*, 107–114, , 2001.
12. Ashburner, M., Ball, C. A., Blake, J. A., Butler, H., Cherry, J. M., Corradi, J., Dolinski, K., Eppig, J. T., Harris, M. A., Hill, D. P., et al. Creating the gene ontology resource: Design and implementation. *Genome Research* 11:1425–1433, 2001.
13. Graph Drawing Software, chapter Graphviz and Dynagraph- Static and Dynamic Graph Drawing. Springer Verlag, 2003.
14. Dwight, S. S., Harris, M. A., Dolinski, K., Ball, C. A., Binkley, G., Christie, K. R., Fisk, D. G., Issel-Tarver, L., Schroeder, M., Sherlock, G., et al. *Saccharomyces* genome database (SGD) provides secondary gene annotation using the gene ontology (GO). *Nucleic Acids Research* 30(1):69–72, 2002.
15. Rice, P., Longden, I., and Bleasby, J. EMBOSS: The european molecular biology open software suite. *Trends in Genetics* 16(6):276–277, June, 2000.

16. Jones, D. T. Protein secondary structure prediction based on position specific scoring matrices. *Journal of Molecular Biology* 292:195–202, 1999.
17. Deng, M., Sun, G., and Chen, T. Assessment of the reliability of protein-protein interactions and protein function prediction. *Pacific Symposium on Biocomputing* 8:140–151, 2003.
18. von Mering, C., Krause, R., Snel, B., Cornell, M., Oliver, S. G., Fields, S. P., and Bork, P. Comparative assessment of large-scale data sets of protein-protein interactions. *Nature* 417:399–403, May, 2002.
19. Fraser, H. B., Hirsh, A. E., Steinmetz, L. M., Scharfe, C., and Feldman, M. W. Evolutionary rate in the protein interaction network. *Science* 296:750–752, April, 2002.
20. Bader, G. D. and Hogue, C. W. V. An automated method for finding molecular complexes in large protein interaction networks. *BMC Bioinformatics* 4(1), 2003.
21. Jones, S. and Thornton, J. M. Principles of protein-protein interactions. *Proceedings of the National Academy of Sciences* 93:13–20, 1996.
22. Veselovsky, A. V., Ivanov, Y. D., Ivanov, A. S., Archakov, A. I., Lewi, P., and Janssen, P. Protein-protein interactions: mechanisms and modification by drugs. *Journal of Molecular Recognition* 15:405–422, 2002.
23. Jones, S., Marin, A., and Thornton, J. M. Protein domain interfaces: characterization and comparison with oligomeric protein interfaces. *Protein Engineering* 13(2):77–82, 2000.
24. Ashburner, M., Ball, C. A., Blake, J. A., Bostein, D., Butler, H., Cherry, J. M., Davis, A. P., Dolinski, K., Dwight, S. S., Eppig, J. T., Harris, M. A., et al. Gene ontology: tool for the unification of biology. *Nature Genetics* 25:25–29, May, 2000.
25. Maniatis, T. and Reed, R. An extensive network of coupling among gene expression machines. *Nature* 416:499–506, April, 2002.
26. Graack, H.-R. and Wittmann-Liebold, B. Mitochondrial ribosomal proteins (MRPs) in yeast. *Biochem J.* 329:433–448, 1998.
27. Reed, R. and Hurt, E. A conserved mRNA export machinery coupled to pre-mRNA splicing. *Cell* 108:523–531, 2002.
28. Keene, J. D. Ribonucleoprotein infrastructure regulating the flow of genetic information between the genome and proteome. *Proceedings of the National Academy of Sciences* 98(13):7018–7024, 2001.
29. Mewes, H., Frishman, D., Guldener, U., Mannhaupt, G., Mayer, K., Mokrejs, M., Morgenstern, B., Musterkoetter, M., Rudd, S., and Weil, B. MIPS: a database for genomes and protein sequences. *Nucleic Acids Research* 30(1):31–34, Jan, 2002.
30. Roth, S. Y., Denu, J. M., and Allis, C. D. Histone acetyltransferases. *Annual Review of Biochemistry* 70:81–120, 2001.
31. Green, C. M. and Almouzni, G. When repair meets chromatin. *EMBO Reports* 3(1):28–33, 2002.
32. Peterson, C. L. Chromatin remodeling enzymes: taming the machines. *EMBO Reports* 3(4):319–322, 2002.